

# Unit 2: Cryptographic Hashing

SI 486I: Randomized and Blockchain Technology

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# Goals of this unit

- Know what a cryptographic hash function is
- Understand the random oracle model of hash functions, why it is useful and what are its limitations
- Understand the three security properties needed for blockchains: collision resistance, hiding, and puzzle-friendliness
- Be able to use these security properties and reason about them
- Know the basic structure of a cryptographic sponge
- Follow the main steps of Keccak hashing for SHA3

# Cryptographic primitives

Primitives are building blocks for crypto protocols.

Examples:

- Hashing
- Signatures
- Encryption

# Big cryptographic principles

These are the law!

- **Don't roll your own crypto** (primitives)
- **The algorithm is not a secret** (Kerckhoffs's principle)
- **Assume attackers are smart, patient, and extremely wealthy**

# Hash function definition

A hash function:

- Takes any amount of input (typically a stream of bytes)
- Produces a fixed-length output (e.g., 32 bytes)
- Is fast to evaluate

Colorful analogy: sausage mixing

Better analogy: (pocketless) billiards

## Algorithm speeds for this class

- Fast
- Slow
- Infeasible

# Probabilities for this class

- Likely
- Unlikely
- “Impossible”

# Desired hash function properties

Assume  $H$  is a hash function with  $n$ -bit outputs.

Collision resistance

No one will ever find  $x_1 \neq x_2$  such that  $H(x_1) = H(x_2)$

Hiding

Given a “random”  $y$ , it is infeasible to find  $x$  such that  $H(x) = y$

Puzzle friendliness

Given a subset  $Y$  of size  $m = \#Y$  of hash digests,

and a “random” prefix  $r$ ,

finding an  $x$  so that  $H(r||x) \in Y$  takes  $O(2^n/m)$  time



## Thought experiment: combining hash functions

Imagine we have two hash functions  $H_1$  and  $H_2$ . One of them is weak but we're not sure which.

We want to combine them into a single strong hash function  $H_3$

Which way(s) will work and which will fail?

- Chaining:  $H_3(x) = H_1(H_2(x))$
- Concatenation:  $H_3(x) = H_1(x) \parallel H_2(x)$
- Bitwise AND:  $H_3(x) = H_1(x) \& H_2(x)$

# Random Oracle Model

Goal: Help us think about how to use strong hash functions

## Santa Claus Hash

- To compute  $H(x)$ , send  $x$  to Santa
- Santa checks his list:
  - If  $x$  is on the list, he returns the listed answer
  - Otherwise, he computes a new, random answer, adds it to the list for the future, and returns it.
- Important: Santa is omnipresent and has perfect memory. (The list contains all previously-hashed values by anyone.)

Note: controversial; subject of serious cryptographic flame wars

# Using ROM

Assume  $H$  is a random oracle with 256-bit outputs.

How do you know  $H$  is:

- Collision resistant?
- Hiding?
- Puzzle friendly?

# Hashing applications

# Hash function standards

- MD5 (Ron Rivest), 1992
- RIPEMD-160 (Belgium), 1992
- SHA-0 (NSA), 1993
- SHA-1 (NSA), 1995
- SHA-2 (NSA), 2001
- BLAKE (Switzerland), 2008
- Keccak (Netherlands), 2008

# Hash function designs

- Merkle-Damgard construction  
Used in MD5, RIPEMD, SHA-1, SHA-2
- Sponge construction  
Used in Keccak (SHA-3)
- Others: HAIFA, Unique Block Iteration, ...

# SHA3-256 details

(aka Keccak[r=1088, c=512])